

ECON 164: Theory of Economic Growth

Week 9A: Natural Resources and the Environment

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 - ...endogenous technological change A wins the race against declining X/L
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 - ...endogenous technological change A wins the race against declining X/L
 - but we treated land as a **renewable resource**: can use the same land over and over
- **today**: **nonrenewable resources** (petroleum, coal, natural gas, minerals, ...)
 - like last time: race between A vs. X/L and E/L
 - quantify the **drag on growth** from **resource extraction**
 - consider relationship between **GDP per capita** and **pollution**

Production with nonrenewables

Production now also requires **land** X and **energy** E :

$$Y_t = K_t^\alpha E_t^\beta X^\gamma (A_t L_t)^{1-\alpha-\beta-\gamma}$$

notice: **constant returns to scale** in $\{K, E, X, L\}$

Capital, labor, and technology growth as in the **Solow** model:

$$\dot{K}_t = s_I Y_t - \delta K_t$$

$$\dot{L}_t = g_L L_t$$

$$\dot{A}_t = g_A A_t$$

Resource extraction

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$$\frac{\dot{R}_t}{R_t} = -\frac{E_t}{R_t}$$

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$$g_R = -s_E \rightarrow g_E = -s_E$$

because $E_t = s_E R_t$

How do we solve this model?

Recall the production function:

$$Y_t = K_t^\alpha E_t^\beta X^\gamma (A_t L_t)^{1-\alpha-\beta-\gamma}$$

If we could instead write...

$$Y_t = K_t^\alpha (B_t L_t)^{1-\alpha}$$

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...would we know what to do?

Yes! This is just the Solow model with **labor-augmenting productivity** B_t ...

- steady state where $g_{\tilde{k}} \equiv g_K - \mathbf{g}_B - g_L = 0 \rightarrow$ phase diagram

$$\tilde{k}^{\text{ss}} = \left(\frac{sI}{\mathbf{g}_B + g_L + \delta} \right)^{\frac{1}{1-\alpha}}$$

- slope of BGP: $g_y^{\text{ss}} = \mathbf{g}_B$

What is B_t ?

Taking ratios of the two possible forms of the production function...

$$1 = \frac{K_t^\alpha E_t^\beta X^\gamma (A_t L_t)^{1-\alpha-\beta-\gamma}}{K_t^\alpha (B_t L_t)^{1-\alpha}} = \frac{E_t^\beta X^\gamma A_t^{1-\alpha-\beta-\gamma} L_t^{-(\beta+\gamma)}}{B_t^{1-\alpha}}$$

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... so we can define B_t as

$$B_t \equiv A_t^{\frac{1-\alpha-\beta-\gamma}{1-\alpha}} \left(\frac{E_t}{L_t} \right)^{\frac{\beta}{1-\alpha}} \left(\frac{X}{L_t} \right)^{\frac{\gamma}{1-\alpha}}$$

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... and its growth rate is then

$$g_B = \frac{1-\alpha-\beta-\gamma}{1-\alpha} g_A + \frac{\beta}{1-\alpha} (g_E - g_L) + \frac{\gamma}{1-\alpha} (g_X - g_L)$$

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Defining the resource drag on growth

We can rearrange the expression for the growth rate of B_t to get...

$$g_y^{ss} = g_B = \left(1 - \frac{\beta + \gamma}{1 - \alpha}\right) g_A - \underbrace{\frac{\beta}{1 - \alpha}(s_E + g_L)}_{\text{drag from energy } E} - \underbrace{\frac{\gamma}{1 - \alpha}g_L}_{\text{drag from land } X}$$

- both include spreading finite resources over more people...
- ...but the drag from **energy** E also includes the depletion of the resource

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Recall: We saw this kind of resource drag at the end of the Malthusian model, too

$$g_y^{\text{ss}} = \beta(g_A^{\text{ss}} - g_L^{\text{ss}}) = (1 - \beta) \frac{\lambda}{1 - \phi} g_L^{\text{ss}} - \underbrace{\beta g_L^{\text{ss}}}_{\text{drag from land } X}$$

- $\alpha \equiv$ share of total factor payments to **capital** $K \approx 0.2$
- $\beta \equiv$ share of total factor payments to **energy** $E \approx 0.1$
- $\gamma \equiv$ share of total factor payments to **land** $X \approx 0.1$

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$$\begin{aligned} -\frac{\beta}{1-\alpha}(s_E + g_L) - \frac{\gamma}{1-\alpha}g_L &= -\left(\frac{0.1}{1-0.2}\right)(\mathbf{0.005} + 0.01) - \left(\frac{0.1}{1-0.2}\right)0.01 \\ &= (1/8) \times 0.015 + (1/8) \times 0.01 \approx \mathbf{0.003} \end{aligned}$$

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→ **1.8% observed growth** includes **0.3% drag** from **energy** and **land**

Comparative statics with respect to s_E

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Say we permanently decrease s_E at time $T \rightarrow$ simul. permanent $g_B \uparrow +$ temp. $B_t \downarrow$

1. What happens to \tilde{k}^{ss} ? **(draw the phase diagram!)**
2. What happens to g_y^{ss} at T ? In the long run?
3. What happens to $\ln y_t^{\text{BGP}}$ at T ? In the long run?

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- **what's the optimal s_E ?** think about analogy w/ s_I and s_R :
 - s_I in **NGM**: more consumption today vs. more consumption tomorrow
 - s_R in **(semi-)endogenous**: more output today vs. more/better ideas for tomorrow

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- **but something's different**: s_E , unlike s_I and s_R , *does* affect the growth rate g_y^{SS}
- **why?** depletion of R is a linear differential equation \rightarrow like **AK models**

How to value “energy today” vs. “resources for tomorrow”

Suppose the representative household has preferences

$$U_t = (c_t - \bar{c})^{1-\rho} R_t^\rho$$

and faces the *implicit* budget constraint

$$y_t = c_t + p_{Rt} R_t$$

- \bar{c} is **subsistence consumption**, like in the Malthusian model
- household cares directly about the **stock of resources** R_t
 - if **resource extraction** implies **pollution** → captures the value of clean environment
 - can reinterpret E_t as **emissions**
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Solving the household's problem

Compute the marginal utility of consumption. . .

$$\text{MU}_c = \frac{(1 - \rho)U_t}{c_t - \bar{c}} = (1 - \rho) \left(\frac{R_t}{c_t - \bar{c}} \right)^\rho$$

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To simplify, let's set $\alpha = \gamma = 0$ to eliminate **capital** (no saving) and **land**...

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... but keep the same resource extraction rule:

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Production and prices

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... but keep the same resource extraction rule:

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Note the tradeoff: more **energy** \rightarrow more **output** y_t but lower **resources** R_t

$$p_{Rt} = \frac{\partial y_t}{\partial E_t}$$

The optimal choice of s_E

Take the household's optimality condition and the price of resources. . .

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The optimal choice of s_E

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$$\frac{\rho}{1-\rho} \left(\frac{c_t - \bar{c}}{R_t} \right) = \beta \frac{y_t}{E_t}$$

...then rearrange to get the optimal choice of s_E :

$$s_E t \equiv \frac{E_t}{R_t} = \beta \left(\frac{1-\rho}{\rho} \right) \frac{y_t}{y_t - \bar{c}}$$

Economic growth leads to better environmental quality

$$sEt = \beta \left(\frac{1 - \rho}{\rho} \right) \frac{y_t}{y_t - \bar{c}}$$

- when y_t is close to subsistence level \bar{c} . . .
 - $y_t/(y_t - \bar{c})$ is high
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 - **think**: electric cars, recycling, low-impact products, . . .

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 - s_E is constant if $\bar{c} = 0 \rightarrow$ what we assumed to start today

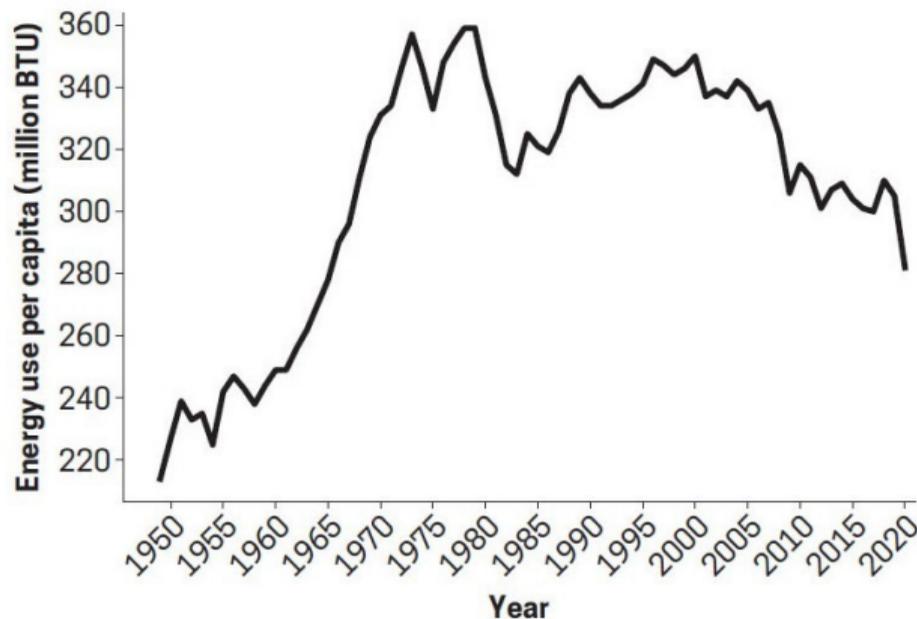
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- requires $\bar{c} > 0$ (nonhomothetic preferences)
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- better model would predict “environmental Kuznets curve” (Brock and Taylor, 2010)
 - s_{Et} rises with y_t at low levels, then falls at high levels

Does economic growth lead to lower resource extraction?

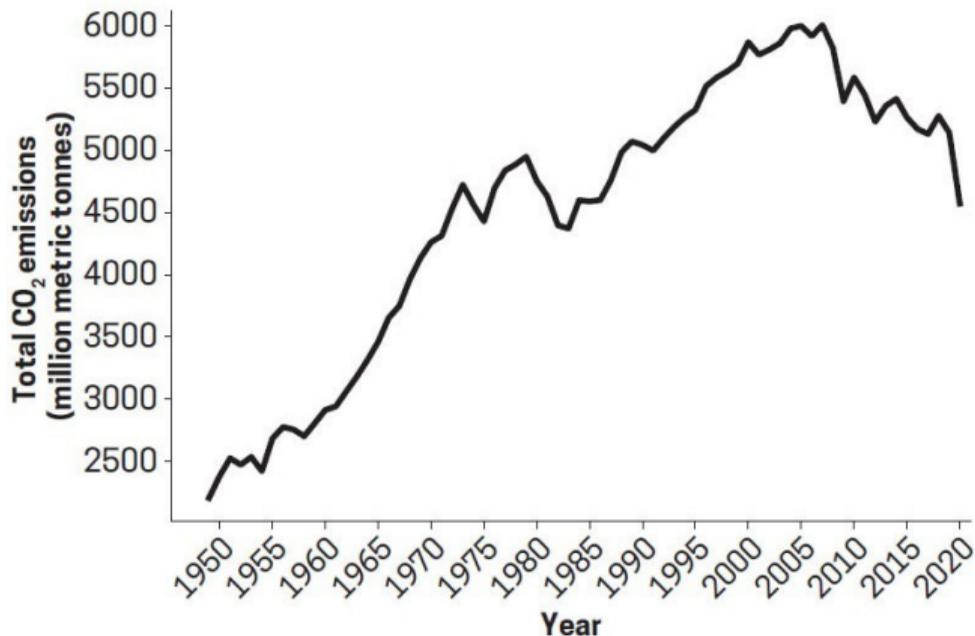
Figure 10.5 Energy Use per Capita in the United States, 1950-2019



SOURCE: Authors' calculations from U.S. Energy Information Administration (2021a).

Does economic growth lead to lower pollution?

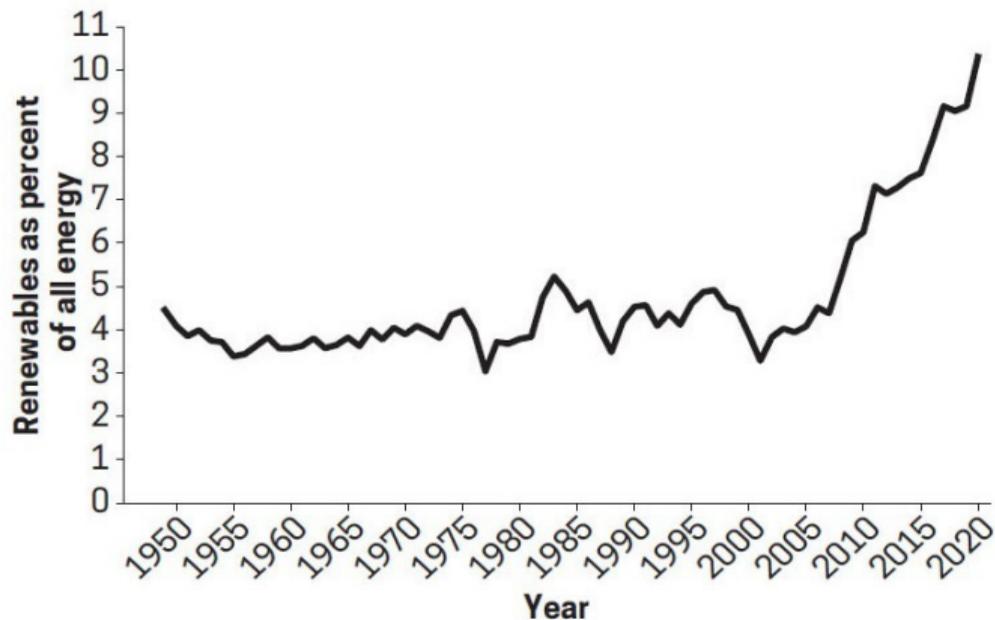
Figure 10.6 Total CO₂ Emissions in the United States, 1950-2019



SOURCE: Authors' calculations from U.S. Energy Information Administration (2021a).

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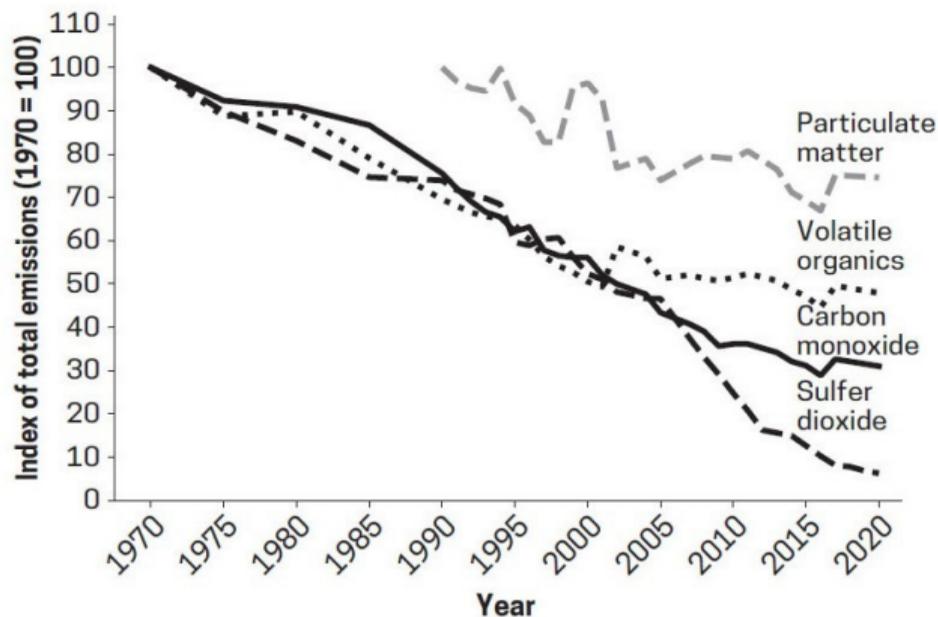
Figure 10.7 Renewables as a Percent of Energy in the United States, 1950-2019



SOURCE: Authors' calculations from U.S. Energy Information Administration (2021a).

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Figure 10.8 Air Pollutants in the United States, 1970–2019



SOURCE: Authors' calculations from U.S. Environmental Protection Agency (2021).

NOTE: The indices for particulate matter are indexed to 100 in 1990, given a lack of prior data. All other series are indexed to 100 in 1970.

Summary

- **last time**: added factor in **fixed supply (land X)** \rightarrow declining GDPpc unless...
 - ...endogenous technological change A wins the race against declining X/L
 - but we treated land as a **renewable resource**: can use the same land over and over
- **today**: **nonrenewable resources** (petroleum, coal, natural gas, minerals, ...)
 - like last time: race between A vs. X/L and E/L
 - can analyze like **Solow model** with **labor-augmenting productivity B_t**
 - find **0.3% drag on growth** from **land** and **resource extraction**
 - some evidence that higher **GDP per capita** leads to lower **emissions s_E**

References

- Brock, William A. and M. Scott Taylor. 2010. "The green Solow model." *Journal of Economic Growth* 15 (2):127–153.
- Dasgupta, Partha and Geoffrey Heal. 1974. "The optimal depletion of exhaustible resources." *Review of Economic Studies* 41 (5):3–28.
- Nordhaus, William D. 1992. "Lethal Model 2: The limits to growth revisited." *Brookings Papers on Economic Activity* 1992 (2):1.